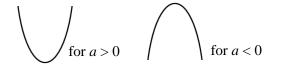
### **Sketching Quadratic Graphs**

#### A LEVEL LINKS

Scheme of work: Ch2-4. Quadratic functions - factorising, solving, graphs and the discriminants

#### **Key points**

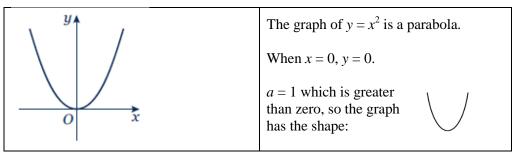
- The graph of the quadratic function  $y = ax^2 + bx + c$ , where  $a \neq 0$ , is a curve called a parabola.
- Parabolas have a line of symmetry and a shape as shown.



- To sketch the graph of a function, find the points where the graph intersects the axes.
- To find where the curve intersects the *y*-axis substitute x = 0 into the function.
- To find where the curve intersects the *x*-axis substitute y = 0 into the function.
- At the turning points of a graph the gradient of the curve is 0 and any tangents to the curve at these points are horizontal.
- To find the coordinates of the maximum or minimum point (turning points) of a quadratic curve (parabola) you can use the completed square form of the function.

#### Examples

**Example 1** Sketch the graph of  $y = x^2$ .



**Example 2** Sketch the graph of  $y = x^2 - x - 6$ .

When $x = 0$ , $y = 0^2 - 0 - 6 = -6$ So the graph intersects the y-axis at $(0, -6)$	1 Find where the graph intersects the <i>y</i> -axis by substituting $x = 0$ .		
When $y = 0$ , $x^2 - x - 6 = 0$	Find where the graph intersects the x-axis by substituting $y = 0$ .		
(x+2)(x-3)=0	<b>3</b> Solve the equation by factorising.		
x = -2  or  x = 3	4 Solve $(x + 2) = 0$ and $(x - 3) = 0$ .		
So, the graph intersects the <i>x</i> -axis at $(-2, 0)$ and $(3, 0)$	a = 1 which is greater than zero, so the graph has the shape:		
	(continued on next page)		
	<b>6</b> To find the turning point, complete		



 $x^{2} - x - 6 = \left(x - \frac{1}{2}\right)^{2} - \frac{1}{4} - 6$   $= \left(x - \frac{1}{2}\right)^{2} - \frac{25}{4}$ When  $\left(x - \frac{1}{2}\right)^{2} = 0$ ,  $x = \frac{1}{2}$  and  $y = -\frac{25}{4}$ , so the turning point is at the point  $\left(\frac{1}{2}, -\frac{25}{4}\right)$   $y = -\frac{25}{4}$   $y = -\frac{25}{4}$  y

#### Practice

- **1** Sketch the graph of  $y = -x^2$ .
- 2 Sketch each graph, labelling where the curve crosses the axes. **a** y = (x+2)(x-1) **b** y = x(x-3) **c** y = (x+1)(x+5)
- 3 Sketch each graph, labelling where the curve crosses the axes.

a	$y = x^2 - x - 6$	b	$y = x^2 - 5x + 4$	c	$y = x^2 - 4$
d	$y = x^2 + 4x$	e	$y = 9 - x^2$	f	$y = x^2 + 2x - 3$

4 Sketch the graph of  $y = 2x^2 + 5x - 3$ , labelling where the curve crosses the axes.

#### Extend

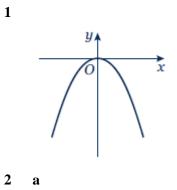
5 Sketch each graph. Label where the curve crosses the axes and write down the coordinates of the turning point.

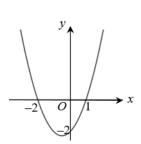
**a**  $y = x^2 - 5x + 6$  **b**  $y = -x^2 + 7x - 12$  **c**  $y = -x^2 + 4x$ 

6 Sketch the graph of  $y = x^2 + 2x + 1$ . Label where the curve crosses the axes and write down the equation of the line of symmetry.



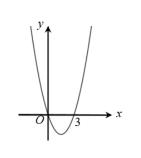
#### Answers

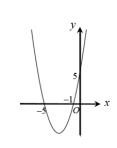




b

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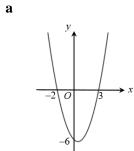


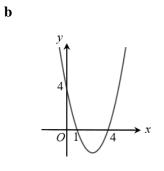


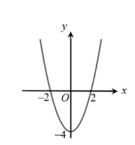
c

с

f

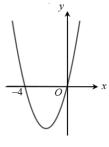


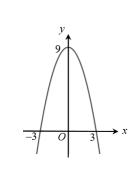


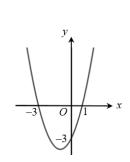




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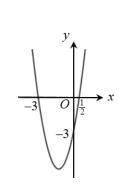


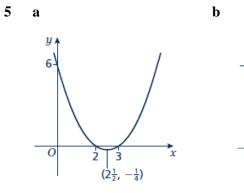


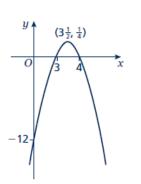


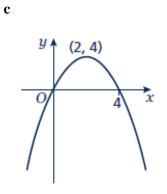


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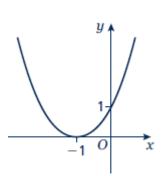












Line of symmetry at x = -1.

