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## **Quadratic Inequalities**

#### A LEVEL LINKS

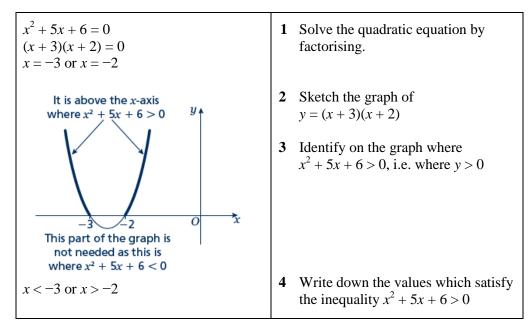
Scheme of work: Ch1-7. Inequalities – linear and quadratic (including graphical solutions)

## **Key points**

- First replace the inequality sign by = and solve the quadratic equation.
- Sketch the graph of the quadratic function.
- Use the graph to find the values which satisfy the quadratic inequality.

### Examples

**Example 1** Find the set of values of x which satisfy  $x^2 + 5x + 6 > 0$ 



**Example 2** Find the set of values of x which satisfy  $x^2 - 5x \le 0$ 

$ \begin{array}{c} x^2 - 5x = 0 \\ x(x - 5) = 0 \\ x = 0 \text{ or } x = 5 \end{array} $	1 Solve the quadratic equation by factorising.
x = 0 or $x = 5$	2 Sketch the graph of $y = x(x-5)$
	3 Identify on the graph where $x^2 - 5x \le 0$ , i.e. where $y \le 0$
$0 \le x \le 5$	4 Write down the values which satisfy the inequality $x^2 - 5x \le 0$



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$-x^{2} - 3x + 10 = 0$ (-x + 2)(x + 5) = 0 x = 2 or x = -5	<b>1</b> Solve the quadratic equation by factorising.
-5 $0$ $2$ $x$	<ul> <li>2 Sketch the graph of y = (-x + 2)(x + 5) = 0</li> <li>3 Identify on the graph where -x<sup>2</sup> - 3x + 10 ≥ 0, i.e. where y ≥ 0</li> </ul>
$-5 \le x \le 2$	3 Write down the values which satisfy the inequality $-x^2 - 3x + 10 \ge 0$

#### **Example 3** Find the set of values of x which satisfy $-x^2 - 3x + 10 \ge 0$

## Practice

- 1 Find the set of values of x for which  $(x + 7)(x 4) \le 0$
- 2 Find the set of values of x for which  $x^2 4x 12 \ge 0$
- **3** Find the set of values of x for which  $2x^2 7x + 3 < 0$
- 4 Find the set of values of x for which  $4x^2 + 4x 3 > 0$
- 5 Find the set of values of x for which  $12 + x x^2 \ge 0$

### Extend

Find the set of values which satisfy the following inequalities.

- $\mathbf{6} \qquad x^2 + x \le \mathbf{6}$
- 7 x(2x-9) < -10
- **8**  $6x^2 \ge 15 + x$



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## Answers

- $1 \quad -7 \le x \le 4$
- $2 \qquad x \le -2 \text{ or } x \ge 6$
- **3**  $\frac{1}{2} < x < 3$
- 4  $x < -\frac{3}{2} \text{ or } x > \frac{1}{2}$
- $5 \quad -3 \le x \le 4$
- $\mathbf{6} \quad -3 \le x \le 2$
- 7  $2 < x < 2\frac{1}{2}$ 8  $x \le -\frac{3}{2}$  or  $x \ge \frac{5}{3}$

