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# AQA Level 2 Certificate FURTHER MATHEMATICS 

Level 2 (8360)

## Worksheet 11

Sequences

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## 11 Sequences

## Question 1

A linear sequence starts

$$
\begin{array}{llll}
250 & 246 & 242 & 238
\end{array}
$$

Which term is the first to have a negative value?

## Question 2

Work out the $n$th term of this quadratic sequence.
8
9
14
23
36
(4 marks)

## Question 3

(a) Show that the $n$th term of the quadratic sequence
$4 \quad 10 \quad 18 \quad 28 \quad \ldots \ldots$ is $n^{2}+3 n$
(3 marks)
(b) Hence, write down the $n$th term of these quadratic sequences.
(b) (i)
$5 \quad 11$
19
29
(1 mark)
(b) (ii)

5
12
21
32
(1 mark)

Question 4 (non calculator)
(a) Write down the $n$th term of the linear sequence
$4 \quad 7 \quad 10 \quad 13$......
(b) Hence, write down the $n$th term of the quadratic sequence.
$1649 \quad 100 \quad 169$......
(c) For the sequence in part 4(b), show that the 30th term is equal to the product of the 2nd and 4th terms

## Question 5



This pattern of rectangles continues.
Show that the sequence of numbers formed by the areas of these rectangles has $n$th term

$$
n^{2}+5 n+6
$$

## Question 6

A linear sequence starts

$$
a+b \quad a+3 b \quad a+5 b \quad a+7 b
$$

The 5th and 8th terms have values 35 and 59 .
(a) Work out $a$ and $b$.
(b) Work out the $n$th term of the sequence.

## Question 7

A sequence has $n$th term $\quad \frac{3 n+1}{n}$
(a) Show that the difference between the $n$th and $(n+1)$ th terms is $\frac{1}{n(n+1)}$
(b) Which are the first two consecutive terms with a difference less than 0.01 ?
(c) Write down the limiting value of the sequence as $n \rightarrow \infty$

## Question 8

A sequence has $n$th term $\frac{5 n+2}{2 n}$
Show that the limiting value of the sequence, $S$, as $n \rightarrow \infty$ is 2.5

## Question 9

Here is the sequence of odd numbers

| 1 | 3 | 5 | 7 | 9 |
| :--- | :--- | :--- | :--- | :--- | :--- |

A quadratic sequence is formed by multiplying consecutive odd numbers in successive pairs.

$$
\begin{array}{llll}
3 & 15 & 35 & 63
\end{array}
$$

Work out the $n$th term of this sequence.

## Question 10

The $n$th term of a sequence is $\frac{2 n^{2}-1}{3 n^{2}+2}$
(a) Show that the difference between the first two terms is $\frac{3}{10}$
(b) Write down the limiting value of the sequence as $n \rightarrow \infty$

