

AQA Qualifications

## AQA Level 2 Certificate FURTHER MATHEMATICS

Level 2 (8365)

Mark Scheme Worksheet 4 Trigonometry Our specification is published on our website (<u>www.aqa.org.uk</u>). We will let centres know in writing about any changes to the specification. We will also publish changes on our website. The definitive version of our specification will always be the one on our website, this may differ from printed versions.

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## **Glossary for Mark Schemes**

These examinations are marked in such a way as to award positive achievement wherever possible. Thus, for these papers, marks are awarded under various categories.

М	Method marks are awarded for a correct method which could lead to a correct answer.	
Α	Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.	
В	Marks awarded independent of method.	
M Dep	A method mark dependent on a previous method mark being awarded.	
B Dep	A mark that can only be awarded if a previous independent mark has been awarded.	
ft	Follow through marks. Marks awarded following a mistake in an earlier step.	
SC	Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.	
oe	Or equivalent. Accept answers that are equivalent.	
	eg, accept 0.5 as well as $\frac{1}{2}$	



## 4 Trigonometry

Question	Answer	Mark	Comments
1	$\sqrt{3/2} + \sqrt{3/2} - 1$	M1	Any 2 values correctly stated in surd form
	$\sqrt{3/2} + \sqrt{3/2} - 1$	M1	All 3 values correctly stated in surd form
	√3 – 1	A1	
2	False	A1	
	True	A1	
	False	A1	
	True	A1	
		D4	
3	Evidence that sin $45^\circ = 1/\sqrt{2}$	B1	
	Area = $\frac{1}{2} \times 5 \times 6\sqrt{2} \times \sin 45^{\circ}$	M1	
	15	A1	
4	sin θ	M1	
	$\tan \theta \equiv \frac{\sin \theta}{\cos \theta} \text{ seen}$		
	$\frac{\sin^2 \theta}{\cos^2 \theta} = \frac{1 - \cos^2 \theta}{\cos^2 \theta}$	M1	
	$\tan \theta = \frac{1}{\cos^2 \theta} - 1$	A1	Accurate method with clear steps is required for all 3 marks
Alt 4	$\frac{1-\cos^2\theta}{\cos^2\theta}$	M1	oe
	$\frac{\sin^2 \theta}{\cos^2 \theta}$	M1	
	$\tan^2 \theta$	A1	Accurate method with clear steps is required for all 3 marks

Question	Answer	Mark	Comments
5	Evidence that angle <i>ADC</i> is a right angle	M1	
	$\sin ACD = \frac{4}{5}$	M1	
	ACD = [53.1, 53.13010235]	A1	Allow 53 with method seen
	Angle ABD = [53.1, 53.13010235]	B1 ft	ft From 3rd mark their angle ACD
6	A triangle formed with <i>A</i> , <i>B</i> and the centre of the hemisphere with 2 sides of 10 cm and an angle of 120°	M1	
	$(AB^2 =) 10^2 + 10^2 - 2 \times 10 \times 10 \times \cos 120$	M1	$2 \times 10 \times sin 60$
	( <i>AB</i> =) [17.3, 17.321]	A1	oe eg, $\sqrt{300}$
	$(\cos AOB =) \frac{30^2 + 30^2 - \text{their } AB^2}{2 \times 30 \times 30}$	M1	$2 \times \sin^{-1}$ (0.5 their <i>AB</i> ÷ 30)
	[33.557, 33.6]	A1 ft	ft Their <i>AB</i>
			Accept 34 with correct method seen
7	$\tan \theta = +\sqrt{2}$ or $\tan \theta = -\sqrt{2}$	M1	
	[54.7,54.74] or [125.26,125.3]	A1	
	180 + their [54.7,54.74] or	M1	
	180 + their [125.26,125.3]		
	[54.7,54.74] and [125.26,125.3] and	A1ft	All 4 solutions
	180 + their [54.7,54.74] and 180 + their [125.26,125.3]		[54.7,54.74] and [125.26,125.3] must be correct
			ft For other two solutions



Question	Answer	Mark	Comments
8	$(3\cos\theta - 1)(\cos\theta + 1)$	M2	M2 Fully correct use of quadratic formula M1 $(a\cos \theta + b)(c\cos \theta + d)$ where $ac = 3$ and $bd = \pm 1$ or quadratic formula with one sign error
	$\cos \theta = -1 \ \text{so} \ \theta = 180^{\circ}$	A1	
	$\cos \theta = \frac{1}{3}  \sin \theta = $ [70.5, 70.53]	A1	
	$\theta = 289.5^{\circ}$	A1 ft	ft 360 – their [70.5, 70.53]
0 (a)		M1	
9 (a)	$\left(\frac{20}{2}\right)^2 + \left(\frac{30}{2}\right)^2$		
	$\sqrt{325}$ or $5\sqrt{13}$ or 18.0(2) or 18.03	A1	
(b)	$\frac{\sin CAB}{\text{their 18.03}} = \frac{\sin 59}{22}$	M1	ое
	$\sin^{-1}\left(\frac{\sin 59}{22} \times \text{their } 18.03\right)$	M1dep	
	44.6	A1	