## AQA

# AQA Level 2 Certificate FURTHER MATHEMATICS 

Level 2 (8365)
Mark Scheme
Worksheet 4
Trigonometry

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## Glossary for Mark Schemes

These examinations are marked in such a way as to award positive achievement wherever possible. Thus, for these papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
M Dep A method mark dependent on a previous method mark being awarded.

B Dep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe Or equivalent. Accept answers that are equivalent.
eg, accept 0.5 as well as $\frac{1}{2}$

## 4 Trigonometry

| Question | Answer | Mark | Comments |
| :--- | :--- | :--- | :--- |
| $\mathbf{1}$ | $\sqrt{3} / 2+\sqrt{ } 3 / 2-1$ | M1 | Any 2 values correctly stated in surd form |
|  | $\sqrt{3} / 2+\sqrt{ } 3 / 2-1$ | M1 | All 3 values correctly stated in surd form |
|  | $\sqrt{3}-1$ | A1 |  |


| $\mathbf{2}$ | False | A1 |  |
| :--- | :--- | :--- | :--- |
|  | True | A1 |  |
|  | False | A1 |  |
|  | True | A1 |  |


| 3 | Evidence that $\sin 45^{\circ}=1 / \sqrt{ } 2$ $\text { Area }=\frac{1}{2} \times 5 \times 6 \sqrt{ } 2 \times \sin 45^{\circ}$ $15$ | B1 <br> M1 <br> A1 |  |
| :---: | :---: | :---: | :---: |
| 4 | $\begin{aligned} & \tan \theta \equiv \frac{\sin \theta}{\cos \theta} \text { seen } \\ & \frac{\sin ^{2} \theta}{\cos ^{2} \theta} \equiv \frac{1-\cos ^{2} \theta}{\cos ^{2} \theta} \\ & \tan \theta \equiv \frac{1}{\cos ^{2} \theta}-1 \end{aligned}$ | M1 <br> M1 <br> A1 | Accurate method with clear steps is required for all 3 marks |
| Alt 4 | $\begin{aligned} & \frac{1-\cos ^{2} \theta}{\cos ^{2} \theta} \\ & \frac{\sin ^{2} \theta}{\cos ^{2} \theta} \\ & \tan ^{2} \theta \end{aligned}$ | M1 <br> M1 <br> A1 | oe <br> Accurate method with clear steps is required for all 3 marks |


| Question | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 5 | Evidence that angle $A D C$ is a right angle $\begin{aligned} & \sin A C D=\frac{4}{5} \\ & A C D=[53.1,53.13010235] \\ & \text { Angle } A B D=[53.1,53.13010235] \end{aligned}$ | M1 <br> M1 <br> A1 <br> B1 ft | Allow 53 with method seen <br> ft From 3rd mark their angle $A C D$ |
| 6 | A triangle formed with $A, B$ and the centre of the hemisphere with 2 sides of 10 cm and an angle of $120^{\circ}$ $\begin{aligned} & \left(A B^{2}=\right) 10^{2}+10^{2}-2 \times 10 \times 10 \times \\ & \cos 120 \\ & (A B=)[17.3,17.321] \\ & (\cos A O B=) \frac{30^{2}+30^{2}-\text { their } A B^{2}}{2 \times 30 \times 30} \end{aligned}$ | M1 <br> M1 <br> A1 <br> M1 <br> A1 ft | $\begin{aligned} & 2 \times 10 \times \sin 60 \\ & \text { oe eg, } \sqrt{300} \\ & 2 \times \sin ^{-1}(0.5 \text { their } A B \div 30) \end{aligned}$ <br> ft Their $A B$ <br> Accept 34 with correct method seen |
| 7 | $\tan \theta=+\sqrt{ } 2$ or $\tan \theta=-\sqrt{ } 2$ <br> [54.7,54.74] or [125.26,125.3] $\begin{aligned} & 180 \text { + their [54.7,54.74] or } \\ & 180 \text { + their [125.26,125.3] } \end{aligned}$ <br> [54.7,54.74] and [125.26,125.3] and 180 + their [54.7,54.74] and <br> 180 + their [ $125.26,125.3$ ] | M1 <br> A1 <br> M1 <br> A1ft | All 4 solutions <br> [54.7,54.74] and [125.26,125.3] must be correct <br> ft For other two solutions |


| Question | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 8 | $\begin{aligned} & (3 \cos \theta-1)(\cos \theta+1) \\ & \cos \theta=-1 \text { so } \theta=180^{\circ} \\ & \cos \theta=\frac{1}{3} \text { so } \theta=[70.5,70.53] \\ & \theta=289.5^{\circ} \end{aligned}$ | M2 <br> A1 <br> A1 <br> A1 ft | M2 Fully correct use of quadratic formula M1 $(a \cos \theta+b)(c \cos \theta+d)$ where $a c=3$ and $b d= \pm 1$ or quadratic formula with one sign error <br> ft 360 - their [70.5, 70.53] |
| $9 \text { (a) }$ <br> (b) | $\begin{aligned} & \left(\frac{20}{2}\right)^{2}+\left(\frac{30}{2}\right)^{2} \\ & \sqrt{325} \text { or } 5 \sqrt{13} \text { or } 18.0(2 \ldots) \text { or } 18.03 \\ & \frac{\sin \mathrm{CAB}}{\text { their } 18.03}=\frac{\sin 59}{22} \\ & \sin ^{-1}\left(\frac{\sin 59}{22} \times \text { their } 18.03\right) \\ & 44.6 \ldots \end{aligned}$ | M1 <br> A1 <br> M1 <br> M1dep <br> A1 | oe |

